

Squares and Square Roots

Question Paper, Set 08

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Write $t \times t$ in power form. [1 mark]
2. Write the square of 22. [1 mark]
3. Find the value of $27^2 - 14^2$. [2 marks]
4. Which number, when squared, gives 2500? [1 mark]
5. Using the rule for numbers ending in 5, find 75^2 . [2 marks]
6. Given $183^2 = 33489$, write the square root of 33489. [1 mark]
7. Find the value of $\sqrt{784} - \sqrt{169}$. [2 marks]
8. Using the prime factorization method, find the square root of 2916. [3 marks]
9. Using the long division method, find the square root of 3721. [3 marks]
10. Find $\sqrt{1521}$ by (i) the prime factorization method (ii) the long division method. [5 marks]
11. Using the long division method, find the square root of 185761. [5 marks]
12. Simplify $\sqrt{18} \times \sqrt{50}$. [2 marks]
13. Find the value of $\sqrt{10} \times \sqrt{10}$. [1 mark]
14. Simplify $\frac{\sqrt{44}}{\sqrt{99}}$. [2 marks]
15. Show that $\frac{17}{\sqrt{17}} = \sqrt{17}$. [1 mark]
16. Verify that $\sqrt{100} + \sqrt{49} \neq \sqrt{100 + 49}$. [3 marks]
17. If $a = 12$ and $b = 16$, show that (i) $\sqrt{a^2 + b^2} \neq a + b$ (ii) $\sqrt{(a + b)^2} = a + b$. [5 marks]
18. Find the square root of 0.0529. [2 marks]
19. Find the square root of 0.001296. [3 marks]
20. Find the square root of 11.56. [5 marks]

Key sheet

Q	Answer
1	t^2
2	484
3	533
4	50
5	5625
6	183
7	15
8	54
9	61
10	39
11	431
12	30
13	10
14	$\frac{2}{3}$
15	$\sqrt{17}$
16	$\text{LHS} = 17 = \sqrt{289}$, $\text{RHS} = \sqrt{149}$; $\text{LHS} \neq \text{RHS}$
17	(i) $20 \neq 28$ (ii) $28 = 28$
18	0.23
19	0.036
20	3.4

Solutions

1. Write $t \times t$ in power form. [1]

t is multiplied by itself 2 times.

$\therefore t \times t = t^2$ (read as 't squared')

Ans: t^2

2. Write the square of 22. [1]

$$22^2 = 22 \times 22$$

$$= 484$$

Ans: 484

3. Find the value of $27^2 - 14^2$. [2]

$$27^2 - 14^2 = 729 - 196$$

$$= 533$$

Ans: 533

4. Which number, when squared, gives 2500? [1]

$$50^2 = 50 \times 50 = 2500$$

$\therefore$ the number is 50

Ans: 50

5. Using the rule for numbers ending in 5, find 75^2 . [2]

The number before 5 is 7: $7 \times 8 = 56$

Write 25 after it.

$$\therefore 75^2 = 5625$$

Ans: 5625

6. Given $183^2 = 33489$, write the square root of 33489. [1]

$$a^2 = b \Rightarrow \sqrt{b} = a$$

$$183^2 = 33489 \Rightarrow \sqrt{33489} = 183$$

Ans: 183

7. Find the value of $\sqrt{784} - \sqrt{169}$. [2]

From the table, $\sqrt{784} = 28$ and $\sqrt{169} = 13$

$$\sqrt{784} - \sqrt{169} = 28 - 13 = 15$$

Ans: 15

8. Using the prime factorization method, find the square root of 2916. [3]

Prime factorization method:

Divide by primes: $2916 \div 2 = 1458$, $1458 \div 2 = 729$, $729 \div 3 = 243$, $243 \div 3 = 81$, $81 \div 3 = 27$, $27 \div 3 = 9$, $9 \div 3 = 3$

$$\begin{aligned}\sqrt{2916} &= \sqrt{(2 \times 2) \times (3 \times 3) \times (3 \times 3) \times (3 \times 3)} \\ &= 2 \times 3 \times 3 \times 3 \\ &= 54\end{aligned}$$

Ans: 54

9. Using the long division method, find the square root of 3721. [3]

Long division method:

Pair the digits from the right: $\overline{37} \overline{21}$

$6 \times 6 = 36 \leq 37$: first digit 6, and $37 - 36 = 1$

Bring down 21: we get 121. New divisor: $6 \times 2 = 12$; $121 \div 12 = 10$ (122 $\times$ 2 = 244 is too big); $121 - 120 = 1$

Remainder 0. $\therefore \sqrt{3721} = 61$

Ans: 61

10. Find $\sqrt{1521}$ by (i) the prime factorization method (ii) the long division method. [5]

(i) Prime factorization method:

Divide by primes: $1521 \div 3 = 507$, $507 \div 3 = 169$, $169 \div 13 = 13$

$$\begin{aligned}\sqrt{1521} &= \sqrt{(3 \times 3) \times (13 \times 13)} \\ &= 3 \times 13 \\ &= 39\end{aligned}$$

(ii) Long division method:

Pair the digits from the right: $\overline{15} \overline{21}$

$3 \times 3 = 9 \leq 15$: first digit 3, and $15 - 9 = 6$

Bring down 21: we get 621. New divisor: $3 \times 2 = 6$; $621 \div 6 = 103$ ($69 \times 9 = 621$); $621 - 621 = 0$

Remainder 0. $\therefore \sqrt{1521} = 39$

Ans: 39

11. Using the long division method, find the square root of 185761. [5]

Long division method:

Pair the digits from the right: $\overline{18} \overline{57} \overline{61}$

$4 \times 4 = 16 \leq 18$: first digit 4, and $18 - 16 = 2$

Bring down 57: we get 257. New divisor: $4 \times 2 = 8$; $83 \times 3 = 249$ ($84 \times 4 = 336$ is too big); $257 - 249 = 8$

Bring down 61: we get 861. New divisor: $43 \times 2 = 86$; $861 \div 86 = 10$ ($862 \times 2 = 1724$ is too big); $861 - 860 = 1$

Remainder 0. $\therefore \sqrt{185761} = 431$

Ans: 431

12. Simplify $\sqrt{18} \times \sqrt{50}$. [2]

$$\sqrt{a} \times \sqrt{b} = \sqrt{a \times b}$$

$$\begin{aligned}\sqrt{18} \times \sqrt{50} &= \sqrt{18 \times 50} = \sqrt{900} \\ &= \sqrt{30 \times 30} = 30\end{aligned}$$

Ans: 30

13. Find the value of $\sqrt{10} \times \sqrt{10}$. [1]

$$\begin{aligned}(\sqrt{a})^2 &= \sqrt{a} \times \sqrt{a} = \sqrt{a^2} = a \\ \therefore \sqrt{10} \times \sqrt{10} &= \sqrt{10^2} = 10\end{aligned}$$

Ans: 10

14. Simplify $\frac{\sqrt{44}}{\sqrt{99}}$. [2]

$$\begin{aligned}\frac{\sqrt{a}}{\sqrt{b}} &= \sqrt{\frac{a}{b}} \\ \frac{\sqrt{44}}{\sqrt{99}} &= \sqrt{\frac{44}{99}} = \sqrt{\frac{11 \times 4}{11 \times 9}} \\ &= \sqrt{\frac{4}{9}} = \frac{2}{3}\end{aligned}$$

Ans: $\frac{2}{3}$

15. Show that $\frac{17}{\sqrt{17}} = \sqrt{17}$. [1]

$$\begin{aligned}17 &= \sqrt{17} \times \sqrt{17} \\ \frac{17}{\sqrt{17}} &= \frac{\sqrt{17} \times \sqrt{17}}{\sqrt{17}} = \sqrt{17}\end{aligned}$$

Ans: $\sqrt{17}$

16. Verify that $\sqrt{100} + \sqrt{49} \neq \sqrt{100 + 49}$. [3]

$$\text{LHS} = \sqrt{100} + \sqrt{49} = 10 + 7 = 17 = \sqrt{289}$$

$$\text{RHS} = \sqrt{100 + 49} = \sqrt{149}$$

$\therefore \text{LHS} \neq \text{RHS}$

Ans: $\text{LHS} = 17 = \sqrt{289}$, $\text{RHS} = \sqrt{149}$; $\text{LHS} \neq \text{RHS}$

17. If $a = 12$ and $b = 16$, show that (i) $\sqrt{a^2 + b^2} \neq a + b$ (ii) $\sqrt{(a + b)^2} = a + b$. [5]

$$\text{(i) LHS} = \sqrt{12^2 + 16^2} = \sqrt{144 + 256} = \sqrt{400} = 20$$

$$\text{RHS} = a + b = 12 + 16 = 28$$

$$20 \neq 28, \text{ so } \sqrt{a^2 + b^2} \neq a + b$$

$$\text{(ii) LHS} = \sqrt{(12 + 16)^2} = \sqrt{28^2} = 28$$

$$\text{RHS} = 12 + 16 = 28$$

$$\text{LHS} = \text{RHS}, \text{ so } \sqrt{(a + b)^2} = a + b$$

Ans: (i) $20 \neq 28$ (ii) $28 = 28$

18. Find the square root of 0.0529. [2]

$$\begin{aligned}\sqrt{0.0529} &= \sqrt{\frac{529}{10000}} \\ &= \frac{\sqrt{529}}{\sqrt{10000}} \\ &= \frac{23}{100} \\ &= 0.23\end{aligned}$$

Ans: 0.23

19. Find the square root of 0.001296. [3]

$$\begin{aligned}\sqrt{0.001296} &= \sqrt{\frac{1296}{1000000}} \\ &= \frac{\sqrt{1296}}{\sqrt{1000000}} \\ 36^2 &= 1296, \text{ so } \sqrt{1296} = 36 \\ &= \frac{36}{1000} \\ &= 0.036\end{aligned}$$

Ans: 0.036

20. Find the square root of 11.56. [5]

$$\sqrt{11.56} = \sqrt{\frac{1156}{100}} = \frac{\sqrt{1156}}{\sqrt{100}}$$

$\sqrt{1156}$ by the long division method:

Pair the digits from the right: $\overline{11} \ \overline{56}$

$3 \times 3 = 9 \leq 11$: first digit 3, and $11 - 9 = 2$

Bring down 56: we get 256. New divisor: $3 \times 2 = 6$; $64 \times 4 = 256$ ($65 \times 5 = 325$ is too big); $256 - 256 = 0$

$$\sqrt{1156} = 34$$

$$\therefore \sqrt{11.56} = \frac{34}{10} = 3.4$$

Ans: 3.4
