

Factorization

MCQ Test, Set 02

Time: 30 minutes

Maximum marks: 25

Name: _____ Class: _____ Date: _____

- There are 25 questions. Each has exactly one correct answer: choose A, B, C or D.
- Each correct answer carries 1 mark. There is no negative marking.
- The key sheet and worked solutions are at the end of this test.

- Factorize $16m^4 - p^4$.
 A. $(2m - p)^2(4m^2 + p^2)$ B. $(2m + p)(2m - p)(4m^2 - p^2)$
 C. $(2m + p)(2m - p)(4m^2 + p^2)$ D. $(2m + p)^2(4m^2 + p^2)$
- The factors of $81t^2 - 64$ are
 A. $(9t + 8)(9t - 8)$ B. $(9t - 8)^2$ C. $(9t + 8)^2$ D. $(81t + 8)(81t - 8)$
- $9a^2 + 30ab + 25b^2 =$
 A. $(3a + 5b)(3a - 5b)$ B. $(5a + 3b)^2$ C. $(3a + 5b)^2$ D. $(3a - 5b)^2$
- The factors of $4x^2 + 20xy + 25y^2$ are
 A. $(2x - 5y)^2$ B. $(2x + 5y)^2$ C. $(5x + 2y)^2$ D. $(2x + 5y)(2x - 5y)$
- The factors of $49m^2 - 70m + 25$ are
 A. $(7m - 5)^2$ B. $(7m + 5)^2$ C. $(5m - 7)^2$ D. $(7m + 5)(7m - 5)$
- Factorize $x^2 - 14x + 49 - 36y^2$.
 A. $(x - 7 - 6y)^2$ B. $(x + 7 + 6y)(x + 7 - 6y)$ C. $(x - 7 + 6y)(x - 7 - 6y)$ D. $(x + 7 - 6y)(x - 7 + 6y)$
- $15a^2 + 22a + 8 =$
 A. $(3a + 2)(5a + 4)$ B. $(3a - 2)(5a - 4)$ C. $(3a - 2)(5a + 4)$ D. $(3a + 4)(5a + 2)$
- To factorize $4p^2 - 7p + 3$ by splitting the middle term, we need two numbers whose product is 4×3 and whose sum is -7 . They are
 A. -6 and -2 B. -12 and -1 C. -3 and -4 D. 3 and 4
- To factorize $5z^2 - 13z + 6$ by splitting the middle term, we need two numbers whose product is 5×6 and whose sum is -13 . They are
 A. 3 and 10 B. -15 and -2 C. -3 and -10 D. -6 and -5
- To factorize $12x^2 + 5x - 3$ by splitting the middle term, we need two numbers whose product is $12 \times (-3)$ and whose sum is 5 . They are
 A. -6 and 6 B. 4 and -9 C. -3 and 12 D. -4 and 9

11. The factors of $19b^2 + 181b + 90$ are
A. $(19b - 10)(b - 9)$ **B.** $(19b - 10)(b + 9)$ **C.** $(19b + 10)(b + 9)$ **D.** $(19b + 9)(b + 10)$
-
12. On factorizing, $-2t - t^2 + 3 =$
A. $(1 - t)(3 - t)$ **B.** $(1 - t)(t + 3)$ **C.** $(t + 3)(t - 1)$ **D.** $(t + 1)(t - 3)$
-
13. On factorizing, $29t - 40 - 3t^2 =$
A. $(3t - 5)(t - 8)$ **B.** $(3t - 5)(8 - t)$ **C.** $(-t - 8)(5 - 3t)$ **D.** $(3t + 5)(t + 8)$
-
14. $3(3a - 4c)^2 + 16(3a - 4c) - 12 =$
A. $(3a - 4c - 6)(9a - 12c - 2)$ **B.** $(3a - 4c - 6)(9a - 12c + 2)$
C. $(3a - 4c + 6)(9a - 12c + 2)$ **D.** $(3a - 4c + 6)(9a - 12c - 2)$
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15. Factorize $5x^2 - 18xy + 9y^2$.
A. $(5x + 3y)(x + 3y)$ **B.** $(5x - 3y)(x - 3y)$ **C.** $(5x - 3y)(x + 3y)$ **D.** $(5x + 3y)(x - 3y)$
-
16. $6\sqrt{2}t^2 - 35t - 3\sqrt{2} =$
A. $(6\sqrt{2}t + 1)(t + 3\sqrt{2})$ **B.** $(6\sqrt{2}t - 1)(t - 3\sqrt{2})$
C. $(6\sqrt{2}t - 1)(t + 3\sqrt{2})$ **D.** $(6\sqrt{2}t + 1)(t - 3\sqrt{2})$
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17. $11a^2 + 6a + \frac{9}{11} =$
A. $(11a + 3)(a + \frac{3}{11})$ **B.** $(11a + 3)(a + 3)$
C. $(11a - 3)(a - \frac{3}{11})$ **D.** $(11a - 3)(a + \frac{3}{11})$
-
18. On factorizing, $3(m + 3)^2 + 13(m + 3)(n + 4) + 4(n + 4)^2 =$
A. $(3m + n + 7)(m + 4n + 7)$ **B.** $(3m + n + 13)(m + 4n + 19)$
C. $(3m + n - 13)(m + 4n + 19)$ **D.** $(3m + n + 13)(m + 4n - 19)$
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19. Factorize $4x^2 + y^2 + 4z^2 + 4xy - 4yz - 8zx$.
A. $(4x + y - 4z)^2$ **B.** $(2x + y + 2z)^2$ **C.** $(-2x + y + 2z)^2$ **D.** $(2x + y - 2z)^2$
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20. On factorizing, $b^3 - 6b^2 + 12b - 8 =$
A. $(b - 2)^3$ **B.** $(b - 2)(b^2 + 2b + 4)$ **C.** $(b + 2)^3$ **D.** $(b + 2)(b - 2)^2$
-
21. $m^3 - 125p^3 =$
A. $(m - 5p)(m^2 + 5mp + 25p^2)$ **B.** $(m - 5p)(m^2 + 10mp + 25p^2)$
C. $(m + 5p)(m^2 - 5mp + 25p^2)$ **D.** $(m - 5p)(m^2 - 5mp + 25p^2)$
-
22. On factorizing, $27 + 64x^3z^3 =$
A. $(16x^2z^2 + 12xz + 9)(3 - 4xz)$ **B.** $(16x^2z^2 - 24xz + 9)(4xz + 3)$
C. $(16x^2z^2 + 12xz + 9)(4xz + 3)$ **D.** $(16x^2z^2 - 12xz + 9)(4xz + 3)$
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23. The factors of $(5m - 3n)^3 + (3n - 2p)^3 + (2p - 5m)^3$ are
- A. $(5m - 3n)(3n - 2p)(2p - 5m)$ B. $3(5m - 3n)(3n - 2p)(2p - 5m)$
C. 0 D. $-3(5m - 3n)(3n - 2p)(2p - 5m)$
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24. On factorizing, $m^5n - 16mn^5 =$
- A. $mn(m + 2n)^2(m - 2n)^2$ B. $mn(m + 2n)^2(m^2 + 4n^2)$
C. $mn(m - 2n)^2(m^2 + 4n^2)$ D. $mn(m + 2n)(m - 2n)(m^2 + 4n^2)$
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25. Factorize $25x^2 + (5x^2 + 3)x + 15$.
- A. $(5x^2 + 5)(x + 3)$ B. $(5x^2 + 3)(x - 5)$ C. $(5x^2 - 3)(x + 5)$ D. $(5x^2 + 3)(x + 5)$
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Key sheet

1. C	2. A	3. C	4. B	5. A
6. C	7. A	8. C	9. C	10. D
11. C	12. B	13. B	14. D	15. B
16. D	17. A	18. B	19. D	20. A
21. A	22. D	23. B	24. D	25. D

Solutions

1. Factorize $16m^4 - p^4$.

$$\begin{aligned}16m^4 - p^4 &= (4m^2)^2 - (p^2)^2 \\&= (4m^2 + p^2)(4m^2 - p^2) \\&= (4m^2 + p^2)[(2m)^2 - p^2] \\&= (4m^2 + p^2)(2m + p)(2m - p)\end{aligned}$$

Ans: (C) $(2m + p)(2m - p)(4m^2 + p^2)$

2. The factors of $81t^2 - 64$ are

$$\begin{aligned}81t^2 - 64 &= (9t)^2 - 8^2 \\&= (9t + 8)(9t - 8) \\&\text{using } a^2 - b^2 = (a + b)(a - b)\end{aligned}$$

Ans: (A) $(9t + 8)(9t - 8)$

3. $9a^2 + 30ab + 25b^2 =$

$$\begin{aligned}9a^2 + 30ab + 25b^2 &= (3a)^2 + (5b)^2 + 2(3a)(5b) \\&= (3a + 5b)^2 \\&= (3a + 5b)(3a + 5b) \\&\text{using } a^2 + b^2 + 2ab = (a + b)^2\end{aligned}$$

Ans: (C) $(3a + 5b)^2$

4. The factors of $4x^2 + 20xy + 25y^2$ are

$$\begin{aligned}4x^2 + 20xy + 25y^2 &= (2x)^2 + (5y)^2 + 2(2x)(5y) \\&= (2x + 5y)^2 \\&= (2x + 5y)(2x + 5y) \\&\text{using } a^2 + b^2 + 2ab = (a + b)^2\end{aligned}$$

Ans: (B) $(2x + 5y)^2$

5. The factors of $49m^2 - 70m + 25$ are

$$\begin{aligned}49m^2 - 70m + 25 &= (7m)^2 + 5^2 - 2(7m)(5) \\&= (7m - 5)^2 \\&= (7m - 5)(7m - 5) \\&\text{using } a^2 + b^2 - 2ab = (a - b)^2\end{aligned}$$

Ans: (A) $(7m - 5)^2$

6. Factorize $x^2 - 14x + 49 - 36y^2$.

$$\begin{aligned}x^2 - 14x + 49 - 36y^2 &= (x - 7)^2 - (6y)^2 \\&= (x - 7 + 6y)(x - 7 - 6y) \\&\text{using } a^2 - 2ab + b^2 = (a - b)^2 \text{ and } a^2 - b^2 = (a + b)(a - b)\end{aligned}$$

Ans: (C) $(x - 7 + 6y)(x - 7 - 6y)$

7. $15a^2 + 22a + 8 =$

$$\begin{aligned}15 \times 8 &= 120: 10 \times 12 = 120 \text{ and } 10 + 12 = 22 \\&= 15a^2 + 10a + 12a + 8 \\&= 5a(3a + 2) + 4(3a + 2) \\&= (3a + 2)(5a + 4)\end{aligned}$$

Ans: (A) $(3a + 2)(5a + 4)$

8. To factorize $4p^2 - 7p + 3$ by splitting the middle term, we need two numbers whose product is 4×3 and whose sum is -7 . They are

$$\begin{aligned}4 \times 3 &= 12 \\(-3) \times (-4) &= 12 \text{ and } -3 - 4 = -7 \\ \text{So the numbers are } &-3 \text{ and } -4.\end{aligned}$$

Ans: (C) -3 and -4

9. To factorize $5z^2 - 13z + 6$ by splitting the middle term, we need two numbers whose product is 5×6 and whose sum is -13 . They are

$$\begin{aligned}5 \times 6 &= 30 \\(-3) \times (-10) &= 30 \text{ and } -3 - 10 = -13 \\ \text{So the numbers are } &-3 \text{ and } -10.\end{aligned}$$

Ans: (C) -3 and -10

10. To factorize $12x^2 + 5x - 3$ by splitting the middle term, we need two numbers whose product is $12 \times (-3)$ and whose sum is 5 . They are

$$\begin{aligned}12 \times (-3) &= -36 \\(-4) \times 9 &= -36 \text{ and } -4 + 9 = 5 \\ \text{So the numbers are } &-4 \text{ and } 9.\end{aligned}$$

Ans: (D) -4 and 9

11. The factors of $19b^2 + 181b + 90$ are

$$\begin{aligned}19 \times 90 &= 1710 \\1710 &= 2 \times 3 \times 3 \times 5 \times 19 = 10 \times 171, \text{ and } 10 + 171 = 181 \\&= 19b^2 + 10b + 171b + 90 \\&= b(19b + 10) + 9(19b + 10) \\&= (19b + 10)(b + 9)\end{aligned}$$

Ans: (C) $(19b + 10)(b + 9)$

12. On factorizing, $-2t - t^2 + 3 =$

$$\begin{aligned}\text{Writing the terms in order: } &-t^2 - 2t + 3 \\(-1) \times 3 &= -3: (-3) \times 1 = -3 \text{ and } -3 + 1 = -2 \\&= -t^2 - 3t + t + 3 \\&= -t(t + 3) + 1(t + 3) \\&= (t + 3)(1 - t)\end{aligned}$$

Ans: (B) $(1 - t)(t + 3)$

13. On factorizing, $29t - 40 - 3t^2 =$

Writing the terms in order: $-3t^2 + 29t - 40$

$$(-3) \times (-40) = 120: 5 \times 24 = 120 \text{ and } 5 + 24 = 29$$

$$= -3t^2 + 5t + 24t - 40$$

$$= -t(3t - 5) + 8(3t - 5)$$

$$= (3t - 5)(8 - t)$$

Ans: (B) $(3t - 5)(8 - t)$

14. $3(3a - 4c)^2 + 16(3a - 4c) - 12 =$

Let $3a - 4c = p$

$$3(3a - 4c)^2 + 16(3a - 4c) - 12 = 3p^2 + 16p - 12$$

$$3 \times (-12) = -36: (-2) \times 18 = -36 \text{ and } -2 + 18 = 16$$

$$= 3p^2 - 2p + 18p - 12$$

$$= p(3p - 2) + 6(3p - 2)$$

$$= (3p - 2)(p + 6)$$

$$= [3(3a - 4c) - 2][(3a - 4c) + 6]$$

$$= (9a - 12c - 2)(3a - 4c + 6)$$

Ans: (D) $(3a - 4c + 6)(9a - 12c - 2)$

15. Factorize $5x^2 - 18xy + 9y^2$.

$$5 \times 9 = 45: (-3) \times (-15) = 45 \text{ and } -3 - 15 = -18$$

$$= 5x^2 - 3xy - 15xy + 9y^2$$

$$= x(5x - 3y) - 3y(5x - 3y)$$

$$= (5x - 3y)(x - 3y)$$

Ans: (B) $(5x - 3y)(x - 3y)$

16. $6\sqrt{2}t^2 - 35t - 3\sqrt{2} =$

$$6\sqrt{2} \times (-3\sqrt{2}) = 6 \times (-3) \times 2 = -36: 1 \times (-36) = -36 \text{ and } 1 - 36 = -35$$

$$= 6\sqrt{2}t^2 + t - 36t - 3\sqrt{2}$$

$$= t(6\sqrt{2}t + 1) - 3\sqrt{2}(6\sqrt{2}t + 1)$$

$$= (6\sqrt{2}t + 1)(t - 3\sqrt{2})$$

Ans: (D) $(6\sqrt{2}t + 1)(t - 3\sqrt{2})$

17. $11a^2 + 6a + \frac{9}{11} =$

$$11a^2 + 6a + \frac{9}{11} = \frac{121a^2 + 66a + 9}{11}$$

$$= \frac{1}{11}(121a^2 + 66a + 9)$$

$$= \frac{1}{11}[(11a)^2 + 3^2 + 2(11a)(3)]$$

$$= \frac{1}{11}(11a + 3)^2$$

$$= \left(a + \frac{3}{11}\right)(11a + 3)$$

Ans: (A) $(11a + 3)\left(a + \frac{3}{11}\right)$

18. On factorizing, $3(m+3)^2 + 13(m+3)(n+4) + 4(n+4)^2 =$

Let $m+3 = x$ and $n+4 = y$

$$3(m+3)^2 + 13(m+3)(n+4) + 4(n+4)^2 = 3x^2 + 13xy + 4y^2$$

$$3 \times 4 = 12: 1 \times 12 = 12 \text{ and } 1 + 12 = 13$$

$$= 3x^2 + xy + 12xy + 4y^2$$

$$= x(3x + y) + 4y(3x + y)$$

$$= (3x + y)(x + 4y)$$

$$= [3(m+3) + (n+4)][(m+3) + 4(n+4)]$$

$$= (3m + 9 + n + 4)(m + 3 + 4n + 16)$$

$$= (3m + n + 13)(m + 4n + 19)$$

Ans: (B) $(3m + n + 13)(m + 4n + 19)$

19. Factorize $4x^2 + y^2 + 4z^2 + 4xy - 4yz - 8zx$.

$$4x^2 + y^2 + 4z^2 + 4xy - 4yz - 8zx = (2x)^2 + y^2 + (2z)^2 + 2(2x)(y) - 2(y)(2z) - 2(2z)(2x)$$

$$= (2x + y - 2z)^2$$

$$\text{using } a^2 + b^2 + c^2 + 2ab - 2bc - 2ca = (a + b - c)^2$$

Ans: (D) $(2x + y - 2z)^2$

20. On factorizing, $b^3 - 6b^2 + 12b - 8 =$

$$b^3 - 6b^2 + 12b - 8 = b^3 - 2^3 - 3(b)^2(2) + 3(b)(2)^2$$

$$= (b - 2)^3$$

$$\text{using } (a - b)^3 = a^3 - b^3 - 3ab(a - b)$$

Ans: (A) $(b - 2)^3$

21. $m^3 - 125p^3 =$

$$m^3 - 125p^3 = m^3 - (5p)^3$$

$$= (m - 5p)[m^2 + (m)(5p) + (5p)^2]$$

$$= (m - 5p)(m^2 + 5mp + 25p^2)$$

$$\text{using } a^3 - b^3 = (a - b)(a^2 + ab + b^2)$$

Ans: (A) $(m - 5p)(m^2 + 5mp + 25p^2)$

22. On factorizing, $27 + 64x^3z^3 =$

$$27 + 64x^3z^3 = 3^3 + (4xz)^3$$

$$= (3 + 4xz)[3^2 - (3)(4xz) + (4xz)^2]$$

$$= (4xz + 3)(16x^2z^2 - 12xz + 9)$$

$$\text{using } a^3 + b^3 = (a + b)(a^2 - ab + b^2)$$

Ans: (D) $(16x^2z^2 - 12xz + 9)(4xz + 3)$

23. The factors of $(5m - 3n)^3 + (3n - 2p)^3 + (2p - 5m)^3$ are

$$\text{Here } (5m - 3n) + (3n - 2p) + (2p - 5m) = 0$$

$$\text{If } a + b + c = 0, \text{ then } a^3 + b^3 + c^3 = 3abc$$

$$\therefore (5m - 3n)^3 + (3n - 2p)^3 + (2p - 5m)^3 = 3(5m - 3n)(3n - 2p)(2p - 5m)$$

Ans: (B) $3(5m - 3n)(3n - 2p)(2p - 5m)$

24. On factorizing, $m^5n - 16mn^5 =$

$$m^5n - 16mn^5 = mn(m^4 - 16n^4)$$

$$= mn[(m^2)^2 - (4n^2)^2]$$

$$= mn(m^2 + 4n^2)(m^2 - 4n^2)$$

$$= mn(m^2 + 4n^2)[m^2 - (2n)^2]$$

$$= mn(m^2 + 4n^2)(m + 2n)(m - 2n)$$

Ans: (D) $mn(m + 2n)(m - 2n)(m^2 + 4n^2)$

25. Factorize $25x^2 + (5x^2 + 3)x + 15$.

$$25x^2 + (5x^2 + 3)x + 15 = 25x^2 + 5x^3 + 3x + 15$$

$$= 5x^3 + 25x^2 + 3x + 15$$

$$= 5x^2(x + 5) + 3(x + 5)$$

$$= (x + 5)(5x^2 + 3)$$

Ans: (D) $(5x^2 + 3)(x + 5)$
