

Decimals and Irrational Numbers

Question Paper, Set 02

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Express $\frac{59}{1000}$ in decimal form. [1 mark]
2. Find the value of $\frac{3.08}{1000}$. [1 mark]
3. Find the value of 0.0526×100 . [1 mark]
4. Write 0070.0200 without the unnecessary zeros. [1 mark]
5. Write the expanded form of 834.926. [2 marks]
6. Find the place value of 5 in 1584.629. [1 mark]
7. Without actual division, write $\frac{11}{8}$ in decimal form. [2 marks]
8. Using the division method, write $\frac{27}{8}$ as a decimal. [3 marks]
9. Without dividing, say whether $\frac{7}{30}$ will be a terminating decimal or a non-terminating repeated decimal. [1 mark]
10. Write $\frac{7}{22}$ in decimal form using the bar notation. [3 marks]
11. Write 0.075 in the form $\frac{p}{q}$ (simplest form). [2 marks]
12. Express $0.\overline{48}$ in the form $\frac{p}{q}$. [3 marks]
13. Express $1.2\overline{45}$ in the form $\frac{p}{q}$ (simplest form). Use the 'let x ' method and check by the short method. [5 marks]
14. Find the sum: $4.087 + 26.35 + 7.6$ [2 marks]
15. Simplify: $1528.4 - 263.057 + 41.93 - 118.6$ [5 marks]
16. Multiply: 0.07×0.006 [2 marks]
17. Divide: $0.0963 \div 3$ [2 marks]
18. Find the value of $\frac{0.072}{0.009}$. [3 marks]
19. Find the value of $\frac{0.2}{0.04} + \frac{0.04}{0.2} - 0.15 \times 4$. [5 marks]

20. Two decimals multiply to give 15.9795. One of them is 2.65. Find the other.

[5 marks]

Key sheet

Q	Answer
1	0.059
2	0.00308
3	5.26
4	70.02
5	$800 + 30 + 4 + \frac{9}{10} + \frac{2}{100} + \frac{6}{1000}$
6	500
7	1.375
8	3.375
9	Non-terminating recurring decimal
10	$0.\overline{318}$
11	$\frac{3}{40}$
12	$\frac{16}{33}$
13	$\frac{137}{110}$
14	38.037
15	1188.673
16	0.00042
17	0.0321
18	8
19	4.6
20	6.03

Solutions

1. Express $\frac{59}{1000}$ in decimal form. [1]

1000 has 3 zeros, so move the decimal point 3 places to the left in 59.

Write zeros in front to fill the empty places.

$$\frac{59}{1000} = 0.059$$

Ans: 0.059

2. Find the value of $\frac{3.08}{1000}$. [1]

Dividing by 1000 moves the decimal point 3 places to the left (put zeros in front where needed).

$$\frac{3.08}{1000} = 0.00308$$

Ans: 0.00308

3. Find the value of 0.0526×100 . [1]

Multiplying by 100 moves the decimal point 2 places to the right (fill zeros if needed).

$$0.0526 \times 100 = 5.26$$

Ans: 5.26

4. Write 0070.0200 without the unnecessary zeros. [1]

Zeros in front of the whole number part and zeros at the end of the decimal part do not change the value.

Zeros in the middle must stay.

$$0070.0200 = 70.02$$

Ans: 70.02

5. Write the expanded form of 834.926. [2]

Place values: $8 \rightarrow 800$, $3 \rightarrow 30$, $4 \rightarrow 4$, $9 \rightarrow \frac{9}{10}$, $2 \rightarrow \frac{2}{100}$, $6 \rightarrow \frac{6}{1000}$

$$834.926 = 800 + 30 + 4 + \frac{9}{10} + \frac{2}{100} + \frac{6}{1000}$$

$$\text{Ans: } 800 + 30 + 4 + \frac{9}{10} + \frac{2}{100} + \frac{6}{1000}$$

6. Find the place value of 5 in 1584.629. [1]

In 1584.629, the digit 5 is in the hundreds place.

Place value of 5 = 500

Ans: 500

7. Without actual division, write $\frac{11}{8}$ in decimal form. [2]

1st method (without actual division)

$8 = 2 \times 2 \times 2$; pair each 2 with a 5 to make 10s.

$$\frac{11}{8} = \frac{11 \times 5 \times 5 \times 5}{2 \times 2 \times 2 \times 5 \times 5 \times 5}$$

$$= \frac{1375}{10 \times 10 \times 10} = \frac{1375}{1000} = 1.375$$

Ans: 1.375

8. Using the division method, write $\frac{27}{8}$ as a decimal. [3]

2nd method (division method): divide 27 by 8.

$$8 \times 3 = 24, 27 - 24 = 3$$

$$\text{Bring down 0: } 30; 8 \times 3 = 24, 30 - 24 = 6$$

$$\text{Bring down 0: } 60; 8 \times 7 = 56, 60 - 56 = 4$$

$$\text{Bring down 0: } 40; 8 \times 5 = 40, 40 - 40 = 0$$

$$\text{Remainder 0. } \therefore \frac{27}{8} = 3.375$$

Ans: 3.375

9. Without dividing, say whether $\frac{7}{30}$ will be a terminating decimal or a non-terminating repeated decimal. [1]

$$30 = 2 \times 3 \times 5 \text{ has the factor 3 (not 2 or 5).}$$

So it is a non-terminating recurring decimal.

Ans: Non-terminating recurring decimal

10. Write $\frac{7}{22}$ in decimal form using the bar notation. [3]

Divide 7 by 22.

$$7 < 22, \text{ so write 0. and bring down a 0}$$

$$\text{Bring down 0: } 70; 22 \times 3 = 66, 70 - 66 = 4$$

$$\text{Bring down 0: } 40; 22 \times 1 = 22, 40 - 22 = 18$$

$$\text{Bring down 0: } 180; 22 \times 8 = 176, 180 - 176 = 4$$

The remainder 4 has come again, so the digits 18 repeat.

$$\therefore \frac{7}{22} = 0.3181818 \dots = 0.3\overline{18}$$

Ans: $0.3\overline{18}$

11. Write 0.075 in the form $\frac{p}{q}$ (simplest form). [2]

$$0.075 = \frac{75}{1000} \text{ (3 digits after the point, so 1000)}$$

$$\text{Divide both by 25: } \frac{75 \div 25}{1000 \div 25} = \frac{3}{40}$$

$$\therefore 0.075 = \frac{3}{40}$$

Ans: $\frac{3}{40}$

12. Express $0.\overline{48}$ in the form $\frac{p}{q}$. [3]

$$\text{Let } x = 0.\overline{48} = 0.484848 \dots$$

$$100x = 48.484848 \dots$$

$$x = 0.484848 \dots$$

$$(-) 99x = 48$$

$$x = \frac{48}{99} = \frac{16}{33}$$

$$\therefore 0.\overline{48} = \frac{16}{33}$$

Ans: $\frac{16}{33}$

13. Express $1.\overline{245}$ in the form $\frac{p}{q}$ (simplest form). Use the 'let x ' method and check by the short method. [5]

$$\text{Let } x = 1.\overline{245} = 1.2454545 \dots$$

$$10x = 12.454545 \dots \text{ (the repeating part starts just after the point)}$$

$$1000x = 1245.454545 \dots$$

$$10x = 12.454545 \dots$$

$$(-) 990x = 1233$$

$$x = \frac{1233}{990} = \frac{137}{110}$$

$$\text{Check (short method): } \frac{1245-12}{990} = \frac{1233}{990} = \frac{137}{110}$$

$$\therefore 1.\overline{245} = \frac{137}{110}$$

$$\text{Ans: } \frac{137}{110}$$

14. Find the sum: $4.087 + 26.35 + 7.6$ [2]

Write the numbers one below the other with the decimal points in a line (fill zeros):

$$\begin{array}{r} 4.087 \\ 26.350 \\ + 7.600 \\ \hline 38.037 \end{array}$$

$$\therefore 4.087 + 26.35 + 7.6 = 38.037$$

$$\text{Ans: } 38.037$$

15. Simplify: $1528.4 - 263.057 + 41.93 - 118.6$ [5]

Group the terms: $(1528.4 + 41.93) - (263.057 + 118.6)$

$$\begin{array}{r} 1528.40 \\ \text{Positive terms: } + 41.93 \\ \hline 1570.33 \end{array}$$

$$\begin{array}{r} 263.057 \\ \text{Negative terms: } + 118.600 \\ \hline 381.657 \end{array}$$

$$\begin{array}{r} 1570.330 \\ \text{Subtract: } - 381.657 \\ \hline 1188.673 \end{array}$$

$$\therefore 1528.4 - 263.057 + 41.93 - 118.6 = 1188.673$$

$$\text{Ans: } 1188.673$$

16. Multiply: 0.07×0.006 [2]

Multiply without the points: $7 \times 6 = 42$

Decimal places: $2 + 3 = 5$

$$0.07 \times 0.006 = 0.00042$$

$$\text{Ans: } 0.00042$$

17. Divide: $0.0963 \div 3$ [2]

$$\frac{0.0963}{3} = \frac{963}{10000 \times 3}$$

$$963 \div 3 = 321$$

$$= \frac{321}{10000} = 0.0321$$

Ans: 0.0321

18. Find the value of $\frac{0.072}{0.009}$. [3]

0.009 has 3 digits after the point, so multiply both by 1000:

$$\frac{0.072}{0.009} = \frac{0.072 \times 1000}{0.009 \times 1000} = \frac{72}{9}$$

$$72 \div 9 = 8$$

$$\therefore 0.072 \div 0.009 = 8$$

Ans: 8

19. Find the value of $\frac{0.2}{0.04} + \frac{0.04}{0.2} - 0.15 \times 4$. [5]

$$\frac{0.2}{0.04} = \frac{0.2 \times 100}{0.04 \times 100} = \frac{20}{4} = 5$$

$$\frac{0.04}{0.2} = \frac{0.04 \times 10}{0.2 \times 10} = \frac{0.4}{2} = 0.2$$

$$0.15 \times 4 = 0.60 = 0.6$$

$$\text{Value} = 5 + 0.2 - 0.6 = 4.6$$

Ans: 4.6

20. Two decimals multiply to give 15.9795. One of them is 2.65. Find the other. [5]

Let the other decimal be x . Then $x \times 2.65 = 15.9795$

$$x = \frac{15.9795}{2.65} = \frac{15.9795 \times 100}{2.65 \times 100} = \frac{1597.95}{265}$$

$$\frac{1597.95}{265} = \frac{159795}{100 \times 265}; \text{ divide 159795 by 265:}$$

$$265 \times 6 = 1590, 1597 - 1590 = 7$$

Bring down 9: $79 < 265$, write 0

$$\text{Bring down 5: } 265 \times 3 = 795, 795 - 795 = 0$$

$$159795 \div 265 = 603, \text{ so } x = \frac{603}{100} = 6.03$$

$$\text{Check: } 6.03 \times 2.65 = 15.9795$$

$$\therefore \text{the other decimal} = 6.03$$

Ans: 6.03
