

Cubes and Cube Roots

Question Paper, Set 04

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Write a^3 as a product. [1 mark]
2. Is 5^3 the same as 5×3 ? Find both values. [2 marks]
3. Find the cube of 4. [1 mark]
4. A big cube is built from small cubes, with 5 small cubes along each edge. How many small cubes are used in all? [2 marks]
5. Fill in the boxes using the table of cubes: (i) $\square^3 = 512$ (ii) $9^3 = \square$ (iii) $\square^3 = 125$ [3 marks]
6. Find the cube of 15. [2 marks]
7. Find 2^3 , 20^3 and 200^3 . How many zeros does 20^3 have more than 2^3 , and 200^3 more than 20^3 ? [5 marks]
8. Without working it out, say whether $(-13)^3$ is positive or negative. Give the reason. [1 mark]
9. Find $(-6)^3$ and $(-10)^3$. [2 marks]
10. Find the cubes of -7 , -9 and -20 . [3 marks]
11. Add the cube of 6 to itself. [1 mark]
12. Three big cubes are built from small cubes, with 3, 4 and 6 small cubes along each edge. How many small cubes are used in all? [5 marks]
13. Find the value of $(-8)^3 + 8^3$. [1 mark]
14. Find the value of $x^3 + (-y)^3$ when $x = 6$ and $y = 2$. [2 marks]
15. What must be added to 4^3 to get 6^3 ? [2 marks]
16. What must be subtracted from 11^3 to get 8^3 ? [3 marks]
17. How much more is 9^3 than $5^3 + 6^3$? [5 marks]
18. Find $(-1)^3 \times 6^3$. [1 mark]

19. If $x = -4$ and $y = 3$, find $x^3 - y^3$. [3 marks]

20. If $a = 4$, $b = -5$ and $c = 3$, find $a^3 + b^3 + c^3$. [5 marks]

Key sheet

Q	Answer
1	$a \times a \times a$
2	No. $5^3 = 125$, but $5 \times 3 = 15$
3	64
4	125 small cubes
5	(i) 8 (ii) 729 (iii) 5
6	3375
7	8, 8000, 8000000; 3 more zeros each time
8	Negative
9	$(-6)^3 = -216$, $(-10)^3 = -1000$
10	$(-7)^3 = -343$, $(-9)^3 = -729$, $(-20)^3 = -8000$
11	432
12	307 small cubes
13	0
14	208
15	152
16	819
17	388
18	-216
19	-91
20	-34

Solutions

1. Write a^3 as a product. [1]

a^3 means a multiplied by itself 3 times.

$$\therefore a^3 = a \times a \times a$$

Ans: $a \times a \times a$

2. Is 5^3 the same as 5×3 ? Find both values. [2]

$$5^3 = 5 \times 5 \times 5 = 125$$

$$5 \times 3 = 15$$

5^3 means 5 multiplied by itself 3 times, not 5 times 3.

Ans: No. $5^3 = 125$, but $5 \times 3 = 15$

3. Find the cube of 4. [1]

$$4^3 = 4 \times 4 \times 4$$

$$= 16 \times 4 = 64$$

Ans: 64

4. A big cube is built from small cubes, with 5 small cubes along each edge. How many small cubes are used in all? [2]

$$\text{Number} = 5 \times 5 \times 5$$

$$= 5^3 = 25 \times 5 = 125$$

Ans: 125 small cubes

5. Fill in the boxes using the table of cubes: (i) $\square^3 = 512$ (ii) $9^3 = \square$ (iii) $\square^3 = 125$ [3]

(i) $8 \times 8 \times 8 = 512$, so the box is 8.

(ii) $9^3 = 9 \times 9 \times 9 = 729$

(iii) $5 \times 5 \times 5 = 125$, so the box is 5.

Ans: (i) 8 (ii) 729 (iii) 5

6. Find the cube of 15. [2]

$$15 \times 15 = 225$$

$$15^3 = 225 \times 15 = 3375$$

Ans: 3375

7. Find 2^3 , 20^3 and 200^3 . How many zeros does 20^3 have more than 2^3 , and 200^3 more than 20^3 ? [5]

$$2^3 = 2 \times 2 \times 2 = 8$$

$$20^3 = 20 \times 20 \times 20 = 400 \times 20 = 8000$$

$$200^3 = 200 \times 200 \times 200 = 40000 \times 200 = 8000000$$

Each time the number is multiplied by 10, its cube gets 3 more zeros.

Ans: 8, 8000, 8000000; 3 more zeros each time

8. Without working it out, say whether $(-13)^3$ is positive or negative. Give the reason. [1]

$$(-13)^3 = -13^3$$

The cube of a negative number is negative.

Ans: Negative

9. Find $(-6)^3$ and $(-10)^3$. [2]

$$(-6)^3 = -6^3 = -216$$

$$10 \times 10 = 100, 100 \times 10 = 1000$$

$$\therefore (-10)^3 = -1000$$

$$\text{Ans: } (-6)^3 = -216, (-10)^3 = -1000$$

10. Find the cubes of -7 , -9 and -20 . [3]

$$(-7)^3 = -7^3 = -(49 \times 7) = -343$$

$$(-9)^3 = -9^3 = -(81 \times 9) = -729$$

$$(-20)^3 = -20^3 = -(400 \times 20) = -8000$$

$$\text{Ans: } (-7)^3 = -343, (-9)^3 = -729, (-20)^3 = -8000$$

11. Add the cube of 6 to itself. [1]

$$6^3 + 6^3 = 216 + 216$$

$$= 432$$

Ans: 432

12. Three big cubes are built from small cubes, with 3, 4 and 6 small cubes along each edge. How many small cubes are used in all? [5]

$$\text{Small cubes used} = 3^3 + 4^3 + 6^3$$

$$3^3 + 4^3 + 6^3 = 27 + 64 + 216$$

$$= 307$$

Ans: 307 small cubes

13. Find the value of $(-8)^3 + 8^3$. [1]

$$(-8)^3 = -8^3$$

$$(-8)^3 + 8^3 = 8^3 - 8^3 = 0$$

Ans: 0

14. Find the value of $x^3 + (-y)^3$ when $x = 6$ and $y = 2$. [2]

$$x^3 + (-y)^3 = 6^3 + (-2)^3$$

$$6^3 + (-2)^3 = 216 + (-8)$$

$$= 216 - 8$$

$$= 208$$

Ans: 208

15. What must be added to 4^3 to get 6^3 ? [2]

$$\text{Number to be added} = 6^3 - 4^3$$

$$6^3 - 4^3 = 216 - 64$$

$$= 152$$

Ans: 152

16. What must be subtracted from 11^3 to get 8^3 ? [3]

$$\text{Number} = 11^3 - 8^3$$

$$11^3 = 121 \times 11 = 1331$$

$$11^3 - 8^3 = 1331 - 512$$

$$= 819$$

Ans: 819

17. How much more is 9^3 than $5^3 + 6^3$? [5]

$$9^3 = 729$$

$$5^3 + 6^3 = 125 + 216 = 341$$

$$\text{Difference} = 729 - 341 = 388$$

Ans: 388

18. Find $(-1)^3 \times 6^3$. [1]

$$(-1)^3 = -1, 6^3 = 216$$

$$-1 \times 216 = -216$$

Ans: -216

19. If $x = -4$ and $y = 3$, find $x^3 - y^3$. [3]

$$x^3 - y^3 = (-4)^3 - 3^3$$

$$(-4)^3 - 3^3 = -64 - 27$$

$$= -91$$

Ans: -91

20. If $a = 4$, $b = -5$ and $c = 3$, find $a^3 + b^3 + c^3$. [5]

$$a^3 + b^3 + c^3 = 4^3 + (-5)^3 + 3^3$$

$$4^3 + (-5)^3 + 3^3 = 64 + (-125) + 27$$

$$= 64 - 125 + 27$$

$$= -34$$

Ans: -34
