

Cubes and Cube Roots

Question Paper, Set 10

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Write $t \times t \times t$ in power form. [1 mark]
2. Write $m \times m \times m \times z \times z \times z$ in power form. [2 marks]
3. Find the value of 2^3 . [1 mark]
4. Is 50 the cube of a whole number? Use the table of cubes. [2 marks]
5. A cube-shaped stack of dice has 5 dice along each edge. (i) How many dice are in the top layer? (ii) How many dice are there in the whole stack? [3 marks]
6. Find 19^3 by first finding 19×19 . [2 marks]
7. Three cube-shaped piles of building blocks have 14, 15 and 40 blocks along each edge. How many blocks does each pile have? [5 marks]
8. Without working it out, say whether $(-11)^3$ is positive or negative. Give the reason. [1 mark]
9. Ravi wrote $(-7)^3 = 343$. Is he right? Write the correct value. [2 marks]
10. Find $(-6)^3$ and 6^3 . Which of the two is bigger, and why? [3 marks]
11. Find $8^3 + 8^3$. [1 mark]
12. Find the sum of the cubes of all the even numbers from 2 to 10. [5 marks]
13. Find the value of $(-25)^3 + 25^3$. [1 mark]
14. Find the value of $x^3 + (-y)^3$ when $x = 4$ and $y = 7$. [2 marks]
15. Ravi found $2^3 - 8^3 = 504$. Is he right? Find the correct answer. [2 marks]
16. Find $13^3 - 10^3$. [3 marks]
17. Simplify $10^3 - 3^3 - 9^3$. [5 marks]
18. Simplify $n^3 - (-n)^3$. [1 mark]
19. Find the value of $(-2)^3 - (-5)^3$. [3 marks]

20. Find $10^3 - 9^3 + 8^3 - 7^3$.

[5 marks]

Key sheet

Q	Answer
1	t^3
2	$m^3 \times z^3$
3	8
4	No, it lies between $3^3 = 27$ and $4^3 = 64$
5	(i) 25 (ii) 125
6	6859
7	2744, 3375, 64000 blocks
8	Negative
9	No. $(-7)^3 = -343$
10	$6^3 = 216$ is bigger than $(-6)^3 = -216$
11	1024
12	1800
13	0
14	-279
15	No. $2^3 - 8^3 = -504$
16	1197
17	244
18	$2n^3$
19	117
20	440

Solutions

1. Write $t \times t \times t$ in power form. [1]

$$t \times t \times t = t^3$$

Read it as 't cubed'.

Ans: t^3

2. Write $m \times m \times m \times z \times z \times z$ in power form. [2]

$$m \times m \times m = m^3$$

$$z \times z \times z = z^3$$

$$\therefore m \times m \times m \times z \times z \times z = m^3 \times z^3$$

Ans: $m^3 \times z^3$

3. Find the value of 2^3 . [1]

$$2^3 = 2 \times 2 \times 2$$

$$= 4 \times 2 = 8$$

Ans: 8

4. Is 50 the cube of a whole number? Use the table of cubes. [2]

From the table: $3^3 = 27$ and $4^3 = 64$.

$27 < 50 < 64$, and no whole number lies between 3 and 4.

So 50 is not a cube.

Ans: No, it lies between $3^3 = 27$ and $4^3 = 64$

5. A cube-shaped stack of dice has 5 dice along each edge. (i) How many dice are in the top layer? (ii) How many dice are there in the whole stack? [3]

(i) One layer has 5 rows of 5: $5 \times 5 = 25$

(ii) There are 5 layers: $25 \times 5 = 125$

So there are $5^3 = 125$ dice.

Ans: (i) 25 (ii) 125

6. Find 19^3 by first finding 19×19 . [2]

$$19 \times 19 = 361$$

$$19^3 = 361 \times 19 = 6859$$

Ans: 6859

7. Three cube-shaped piles of building blocks have 14, 15 and 40 blocks along each edge. How many blocks does each pile have? [5]

$$\text{Edge 14: } 14 \times 14 = 196, 196 \times 14 = 2744$$

$$\text{Edge 15: } 15 \times 15 = 225, 225 \times 15 = 3375$$

$$\text{Edge 40: } 40 \times 40 = 1600, 1600 \times 40 = 64000$$

Ans: 2744, 3375, 64000 blocks

8. Without working it out, say whether $(-11)^3$ is positive or negative. Give the reason. [1]

$$(-11)^3 = -11^3$$

The cube of a negative number is negative.

Ans: Negative

9. Ravi wrote $(-7)^3 = 343$. Is he right? Write the correct value. [2]

$$(-7)^3 = (-7) \times (-7) \times (-7)$$

$$= 49 \times (-7) = -343$$

A negative number multiplied 3 times gives a negative answer, so Ravi is wrong.

Ans: No. $(-7)^3 = -343$

10. Find $(-6)^3$ and 6^3 . Which of the two is bigger, and why? [3]

$$6^3 = 6 \times 6 \times 6 = 216$$

$$(-6)^3 = (-6) \times (-6) \times (-6) = -216$$

216 is positive and -216 is negative, so 6^3 is bigger.

Ans: $6^3 = 216$ is bigger than $(-6)^3 = -216$

11. Find $8^3 + 8^3$. [1]

$$8^3 + 8^3 = 512 + 512$$

$$= 1024$$

Ans: 1024

12. Find the sum of the cubes of all the even numbers from 2 to 10. [5]

$$2^3 + 4^3 + 6^3 + 8^3 + 10^3 = 8 + 64 + 216 + 512 + 1000$$

$$= 1800$$

Ans: 1800

13. Find the value of $(-25)^3 + 25^3$. [1]

$$(-25)^3 = -25^3$$

$$(-25)^3 + 25^3 = 25^3 - 25^3 = 0$$

Ans: 0

14. Find the value of $x^3 + (-y)^3$ when $x = 4$ and $y = 7$. [2]

$$x^3 + (-y)^3 = 4^3 + (-7)^3$$

$$4^3 + (-7)^3 = 64 + (-343)$$

$$= 64 - 343$$

$$= -279$$

Ans: -279

15. Ravi found $2^3 - 8^3 = 504$. Is he right? Find the correct answer. [2]

$$2^3 - 8^3 = 8 - 512$$

We take away the bigger number 512 from the smaller number 8, so the answer is negative.

$$8 - 512 = -504$$

Ravi subtracted the other way round; the correct answer is -504 .

Ans: No. $2^3 - 8^3 = -504$

16. Find $13^3 - 10^3$. [3]

$$13^3 = 169 \times 13 = 2197$$

$$13^3 - 10^3 = 2197 - 1000$$

$$= 1197$$

Ans: 1197

17. Simplify $10^3 - 3^3 - 9^3$. [5]

$$10^3 - 3^3 - 9^3 = 1000 - 27 - 729$$

$$= 244$$

Ans: 244

18. Simplify $n^3 - (-n)^3$. [1]

$$(-n)^3 = -n^3$$

$$n^3 - (-n^3) = n^3 + n^3 = 2n^3$$

Ans: $2n^3$

19. Find the value of $(-2)^3 - (-5)^3$. [3]

$$(-2)^3 - (-5)^3 = -8 - (-125)$$

$$= -8 + 125$$

$$= 117$$

Ans: 117

20. Find $10^3 - 9^3 + 8^3 - 7^3$. [5]

$$10^3 - 9^3 + 8^3 - 7^3 = 1000 - 729 + 512 - 343$$

$$= 440$$

Ans: 440
