

Arithmetic (Level 1)

Question Paper, Set 04

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Express 45 : 75 in its simplest form. [1 mark]
2. Divide ₹4500 among three friends in the ratio 1 : 3 : 5. [3 marks]
3. Are 4, 9, 12, 27 in proportion? Give a reason. [1 mark]
4. Find the mean proportional between 9 and 16. [1 mark]
5. If $\frac{x}{y} = \frac{9}{4}$, find $\frac{x+y}{y}$. [2 marks]
6. An electric pole 9 m high casts a shadow of 6 m. Find the height of a tree that casts a shadow of 10 m under similar conditions. [2 marks]
7. There is food for 600 men for 25 days. After 5 days, how many more men should join so that the remaining food lasts for 16 more days? [5 marks]
8. Express 0.065 as a percentage. [1 mark]
9. What percent of 25 is 7? [1 mark]
10. The price of a mixer is ₹1350. It is decreased by 6%. Find the new price. [2 marks]
11. The present population of a city is 13,310. It has been increasing at the rate of 10% per annum. Find its population 3 years ago. [3 marks]
12. By selling an article for ₹612, a man loses 15%. Find the cost price. [2 marks]
13. A shopkeeper marks an article costing ₹600 at 30% above its cost price and then gives a discount of 10%. Find the marked price, the selling price and the profit percentage. [5 marks]
14. If the cost price of 12 articles is equal to the selling price of 15 articles, find the gain or loss percent. [3 marks]
15. Find the average of 48, 52, 61, 39. [1 mark]
16. A bus travels from town A to town B at 45 km/h. It covers one-fourth of the total distance in 3 hours. Find the distance between A and B. [2 marks]

- 17.** A car takes one-third of the time taken by a bus for the same journey. The bus takes 15 hours. If the speed of the car is 75 km/h, find the speed of the bus. [2 marks]
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- 18.** A train 150 m long crosses an electric pole in 9 seconds. Find its speed in km/h. [3 marks]
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- 19.** The simple interest is ₹243 and the amount is ₹1143 at 6% per annum. Find the principal and the time. [5 marks]
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- 20.** In a factory, the production of scooters rose from 25,000 to 28,090 in 2 years. Find the rate of growth per annum. [5 marks]
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Key sheet

Q	Answer
1	3 : 5
2	₹500, ₹1500, ₹2500
3	Yes
4	12
5	$\frac{13}{4}$
6	15 m
7	150 more men
8	6.5%
9	28%
10	₹1269
11	10,000
12	₹720
13	M.P ₹780; S.P ₹702; profit 17%
14	Loss of 20%
15	50
16	540 km
17	25 km/h
18	60 km/h
19	Principal ₹900; time $4\frac{1}{2}$ years
20	6% per annum

Solutions

1. Express 45 : 75 in its simplest form. [1]

H.C.F of 45 and 75 is 15.

$$\frac{45}{75} = \frac{15 \times 3}{15 \times 5} = \frac{3}{5}$$

Simplest form = 3 : 5

Ans: 3 : 5

2. Divide ₹4500 among three friends in the ratio 1 : 3 : 5. [3]

Sum of the terms of the ratio = $1 + 3 + 5 = 9$

$$\text{1st share} = \frac{1}{9} \times 4500 = 500$$

$$\text{2nd share} = \frac{3}{9} \times 4500 = 1500$$

$$\text{3rd share} = \frac{5}{9} \times 4500 = 2500$$

Ans: ₹500, ₹1500, ₹2500

3. Are 4, 9, 12, 27 in proportion? Give a reason. [1]

$$\text{Product of extremes} = 4 \times 27 = 108$$

$$\text{Product of means} = 9 \times 12 = 108$$

They are equal, so $4 : 9 :: 12 : 27$. Yes.

Ans: Yes

4. Find the mean proportional between 9 and 16. [1]

$$\text{Mean proportional} = \sqrt{9 \times 16} = \sqrt{144} = 12$$

Ans: 12

5. If $\frac{x}{y} = \frac{9}{4}$, find $\frac{x+y}{y}$. [2]

By componendo, if $\frac{a}{b} = \frac{c}{d}$ then $\frac{a+b}{b} = \frac{c+d}{d}$.

$$\frac{x+y}{y} = \frac{9+4}{4} = \frac{13}{4}$$

Ans: $\frac{13}{4}$

6. An electric pole 9 m high casts a shadow of 6 m. Find the height of a tree that casts a shadow of 10 m under similar conditions. [2]

Shadow (m) | Height (m)

$$6 \mid 9$$

$$10 \mid y$$

Direct proportion: $x_1 y_2 = x_2 y_1$

$$6 \times y = 10 \times 9 \Rightarrow y = \frac{10 \times 9}{6} = 15$$

Ans: 15 m

7. There is food for 600 men for 25 days. After 5 days, how many more men should join so that the remaining food lasts for 16 more days? [5]

$$\text{Total food} = 600 \times 25 = 15,000 \text{ man-days}$$

$$\text{Food used in 5 days} = 600 \times 5 = 3000 \text{ man-days}$$

$$\text{Remaining food} = 15,000 - 3000 = 12,000$$

$$\text{Men it can feed for 16 days} = \frac{12,000}{16} = 750$$

$$\text{More men} = 750 - 600 = 150$$

Ans: 150 more men

8. Express 0.065 as a percentage. [1]

$$0.065 = (0.065 \times 100)\% = 6.5\%$$

Ans: 6.5%

9. What percent of 25 is 7? [1]

$$\left(\frac{7}{25} \times 100\right)\% = 28\%$$

Ans: 28%

10. The price of a mixer is ₹1350. It is decreased by 6%. Find the new price. [2]

$$\text{Final value after an decrease of } 6\% = \left(\frac{100-R}{100}\right) P$$

$$= \frac{100-6}{100} \times 1350 = \frac{94}{100} \times 1350 = 1269$$

Ans: ₹1269

11. The present population of a city is 13,310. It has been increasing at the rate of 10% per annum. Find its population 3 years ago. [3]

$$\text{Population } n \text{ years ago} = \frac{P}{\left(1 + \frac{R}{100}\right)^n}$$

$$= \frac{13,310}{\left(1 + \frac{10}{100}\right)^3} = \frac{13,310}{\left(\frac{11}{10}\right)^3}$$

$$= 13,310 \times \frac{10}{11} \times \frac{10}{11} \times \frac{10}{11} = 10,000$$

Ans: 10,000

12. By selling an article for ₹612, a man loses 15%. Find the cost price. [2]

$$\text{C.P} = \frac{100}{100 - \text{Loss}\%} \times \text{S.P}$$

$$= \frac{100}{100-15} \times 612 = \frac{100}{85} \times 612 = 720$$

Ans: ₹720

13. A shopkeeper marks an article costing ₹600 at 30% above its cost price and then gives a discount of 10%. Find the marked price, the selling price and the profit percentage. [5]

$$\text{M.P} = 600 + 30\% \text{ of } 600 = 780$$

$$\text{S.P} = \frac{100-10}{100} \times 780 = 702$$

$$\text{Profit} = 702 - 600 = 102$$

$$\text{Profit \%} = \left(\frac{102}{600} \times 100\right)\% = 17\%$$

Ans: M.P ₹780; S.P ₹702; profit 17%

14. If the cost price of 12 articles is equal to the selling price of 15 articles, find the gain or loss percent. [3]

Let C.P of each = x and S.P of each = y .

$$12x = 15y \Rightarrow \frac{y}{x} = \frac{12}{15} = \frac{4}{5}$$

$y < x$, so there is a loss.

$$\text{Loss \%} = \left(1 - \frac{y}{x}\right) \times 100 = 20\%$$

Ans: Loss of 20%

15. Find the average of 48, 52, 61, 39. [1]

$$\begin{aligned}\text{Average} &= \frac{\text{Sum of observations}}{\text{No. of observations}} \\ &= \frac{48+52+61+39}{4} = \frac{200}{4} = 50\end{aligned}$$

Ans: 50

16. A bus travels from town A to town B at 45 km/h. It covers one-fourth of the total distance in 3 hours. Find the distance between A and B. [2]

Let $AB = x$. It covers $\frac{x}{4}$ in 3 h.

$$S = \frac{D}{T} \Rightarrow 45 = \frac{x/4}{3}$$

$$\Rightarrow x = 45 \times 3 \times 4 = 540 \text{ km}$$

Ans: 540 km

17. A car takes one-third of the time taken by a bus for the same journey. The bus takes 15 hours. If the speed of the car is 75 km/h, find the speed of the bus. [2]

$$\frac{T_1}{T_2} = \frac{1}{3} \text{ (} T_1 \text{ for the car, } T_2 \text{ for the bus)}$$

$$s_1 : s_2 = T_2 : T_1 = 3 : 1$$

$$\text{Speed of bus} = \frac{75}{3} = 25 \text{ km/h}$$

Ans: 25 km/h

18. A train 150 m long crosses an electric pole in 9 seconds. Find its speed in km/h. [3]

To cross a pole, the train travels its own length.

$$S = \frac{D}{T} = \frac{150}{9} = 16\frac{2}{3} \text{ m/s}$$

$$= 16\frac{2}{3} \times \frac{18}{5} = 60 \text{ km/h}$$

Ans: 60 km/h

19. The simple interest is ₹243 and the amount is ₹1143 at 6% per annum. Find the principal and the time. [5]

$$\text{Amount} = P + \text{S.I} \Rightarrow 1143 = P + 243$$

$$P = 1143 - 243 = 900$$

$$\text{S.I} = \frac{P \times T \times R}{100} \Rightarrow 243 = \frac{900 \times T \times 6}{100}$$

$$T = \frac{243 \times 100}{900 \times 6} = 4\frac{1}{2} \text{ years}$$

Ans: Principal ₹900; time $4\frac{1}{2}$ years

20. In a factory, the production of scooters rose from 25,000 to 28,090 in 2 years. Find the rate of growth per annum. [5]

$$A = P \left(1 + \frac{R}{100}\right)^n$$

$$28,090 = 25,000 \left(1 + \frac{R}{100}\right)^2$$

$$\Rightarrow \left(1 + \frac{R}{100}\right)^2 = \frac{28,090}{25,000} = \frac{2809}{2500} = \left(\frac{53}{50}\right)^2$$

$$\Rightarrow 1 + \frac{R}{100} = \frac{53}{50} \Rightarrow \frac{R}{100} = \frac{3}{50}$$

$$\Rightarrow R = 6\%$$

Ans: 6% per annum
