

Arithmetic (Level 1)**Question Paper, Set 10**

Time: 1 hour 30 minutes

Maximum marks: 50

Name: _____ Class: _____ Date: _____

1. Answer all 20 questions. The marks for each question are shown in brackets.
2. Show your working for the 2, 3 and 5 mark questions.
3. The key sheet and worked solutions are at the end of this paper.

1. Find the ratio of 8 months to 3 years in its simplest form. [1 mark]
2. Divide ₹6300 among three sisters in the ratio 5 : 6 : 7. [3 marks]
3. Find the fourth proportional to 9, 15 and 12. [1 mark]
4. Find the mean proportional between 16 and 81. [1 mark]
5. If $\frac{a}{b} = \frac{c}{d} = \frac{2}{5}$, find the value of $\frac{3a+4c}{3b+4d}$. [2 marks]
6. A photograph of a microbe enlarged 20,000 times has a length of 4 cm. What is the actual length of the microbe? [2 marks]
7. 36 men can finish a piece of work in 25 days. After 10 days, 9 men leave. In how many days will the remaining men finish the rest of the work? [5 marks]
8. Express 45% as a fraction in its simplest form. [1 mark]
9. Find 2.5% of 640. [1 mark]
10. A number 480 is increased by 25%. Find the new number. [2 marks]
11. The present population of a city is 21,632. It has been increasing at the rate of 4% per annum. Find its population 2 years ago. [3 marks]
12. An agent gets a commission of 4% on his sales. If on a certain day he gets ₹180 as commission, find the worth of the goods sold through him that day. [2 marks]
13. A shopkeeper sells a lamp marked at ₹960 at a discount of 25% and suffers a loss of 10%. Find the discount, the selling price, the cost price and the loss. [5 marks]
14. If the cost price of 10 articles is equal to the selling price of 8 articles, find the gain or loss percent. [3 marks]
15. The average of 25 numbers is 36.4. Find their sum. [1 mark]
16. A scooter covers 168 km in 4 hours. How much distance will it cover in 7 hours at the same speed? [2 marks]

- 17.** The speed of Sneha is 35 km/h and the speed of Priya is 56 km/h. Find the ratio of the times taken by them to cover the same distance. [2 marks]
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- 18.** A train running at 90 km/h crosses a signal post in 12 seconds. Find the length of the train. [3 marks]
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- 19.** Find the interest on ₹6000 for 2 years at 10% per annum (i) as simple interest, (ii) as compound interest, working year by year. [5 marks]
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- 20.** A sum of ₹6400 amounts to ₹7225 in 2 years at compound interest, compounded annually. Find the rate of interest per annum. [5 marks]
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Key sheet

Q	Answer
1	2 : 9
2	₹1750, ₹2100, ₹2450
3	20
4	36
5	$\frac{2}{5}$
6	$\frac{1}{5000}$ cm
7	20 days
8	$\frac{9}{20}$
9	16
10	600
11	20,000
12	₹4500
13	Discount ₹240; S.P ₹720; C.P ₹800; loss ₹80
14	Gain of 25%
15	910
16	294 km
17	8 : 5
18	300 m
19	(i) ₹1200 (ii) ₹1260
20	6.25% per annum

Solutions

1. Find the ratio of 8 months to 3 years in its simplest form. [1]

$$3 \text{ years} = 3 \times 12 \text{ months} = 36 \text{ months}$$

$$\frac{8 \text{ months}}{36 \text{ months}} = \frac{8}{36} = \frac{2}{9}$$

$$\text{Ratio} = 2 : 9$$

$$\text{Ans: } 2 : 9$$

2. Divide ₹6300 among three sisters in the ratio 5 : 6 : 7. [3]

$$\text{Sum of the terms of the ratio} = 5 + 6 + 7 = 18$$

$$\text{1st share} = \frac{5}{18} \times 6300 = 1750$$

$$\text{2nd share} = \frac{6}{18} \times 6300 = 2100$$

$$\text{3rd share} = \frac{7}{18} \times 6300 = 2450$$

$$\text{Ans: ₹1750, ₹2100, ₹2450}$$

3. Find the fourth proportional to 9, 15 and 12. [1]

Let the fourth proportional be x . Then $9 : 15 :: 12 : x$.

$$9 \times x = 15 \times 12$$

$$x = \frac{15 \times 12}{9} = 20$$

$$\text{Ans: } 20$$

4. Find the mean proportional between 16 and 81. [1]

$$\text{Mean proportional} = \sqrt{16 \times 81} = \sqrt{1296} = 36$$

$$\text{Ans: } 36$$

5. If $\frac{a}{b} = \frac{c}{d} = \frac{2}{5}$, find the value of $\frac{3a+4c}{3b+4d}$. [2]

$$\text{If } \frac{a}{b} = \frac{c}{d} \text{ then } \frac{a}{b} = \frac{c}{d} = \frac{al+cm}{bl+dm}.$$

$$\text{Here } l = 3, m = 4, \text{ so } \frac{3a+4c}{3b+4d} = \frac{a}{b} = \frac{2}{5}$$

$$\text{Ans: } \frac{2}{5}$$

6. A photograph of a microbe enlarged 20,000 times has a length of 4 cm. What is the actual length of the microbe? [2]

Times enlarged | Length (cm)

$$20,000 \mid 4$$

$$1 \mid y$$

$$\text{Direct proportion: } x_1 y_2 = x_2 y_1$$

$$20,000 \times y = 1 \times 4 \Rightarrow y = \frac{1 \times 4}{20,000} = \frac{1}{5000}$$

$$\frac{1}{5000} \text{ cm} = 0.0002 \text{ cm} = 2 \times 10^{-4} \text{ cm}$$

$$\text{Ans: } \frac{1}{5000} \text{ cm}$$

7. 36 men can finish a piece of work in 25 days. After 10 days, 9 men leave. In how many days will the remaining men finish the rest of the work? [5]

Work left = work of 36 men for $25 - 10 = 15$ days

Men now = $36 - 9 = 27$

Men and days are in inverse proportion: $x_1y_1 = x_2y_2$

$$36 \times 15 = 27 \times y \Rightarrow y = \frac{540}{27} = 20$$

Ans: 20 days

8. Express 45% as a fraction in its simplest form. [1]

$$45\% = \frac{45}{100} = \frac{9}{20}$$

Ans: $\frac{9}{20}$

9. Find 2.5% of 640. [1]

$$2.5\% \text{ of } 640 = \frac{2.5}{100} \times 640 = 16$$

Ans: 16

10. A number 480 is increased by 25%. Find the new number. [2]

Final value after an increase of 25% = $\left(\frac{100+R}{100}\right)P$

$$= \frac{100+25}{100} \times 480 = \frac{125}{100} \times 480 = 600$$

Ans: 600

11. The present population of a city is 21,632. It has been increasing at the rate of 4% per annum. Find its population 2 years ago. [3]

$$\text{Population } n \text{ years ago} = \frac{P}{\left(1 + \frac{R}{100}\right)^n}$$

$$= \frac{21,632}{\left(1 + \frac{4}{100}\right)^2} = \frac{21,632}{\left(\frac{26}{25}\right)^2}$$

$$= 21,632 \times \frac{25}{26} \times \frac{25}{26} = 20,000$$

Ans: 20,000

12. An agent gets a commission of 4% on his sales. If on a certain day he gets ₹180 as commission, find the worth of the goods sold through him that day. [2]

Let the total sales be ₹ x .

$$4\% \text{ of } x = 180 \Rightarrow \frac{4}{100}x = 180$$

$$x = \frac{180 \times 100}{4} = 4500$$

Ans: ₹4500

13. A shopkeeper sells a lamp marked at ₹960 at a discount of 25% and suffers a loss of 10%. Find the discount, the selling price, the cost price and the loss. [5]

$$\text{Discount} = 25\% \text{ of } 960 = 240$$

$$\text{S.P} = 960 - 240 = 720$$

$$\text{C.P} = \frac{100}{100 - \text{Loss}\%} \times \text{S.P}$$

$$= \frac{100}{90} \times 720 = 800$$

$$\text{Loss} = 800 - 720 = 80$$

Ans: Discount ₹240; S.P ₹720; C.P ₹800; loss ₹80

14. If the cost price of 10 articles is equal to the selling price of 8 articles, find the gain or loss percent. [3]

Let C.P of each = x and S.P of each = y .

$$10x = 8y \Rightarrow \frac{y}{x} = \frac{10}{8} = \frac{5}{4}$$

$y > x$, so there is a gain.

$$\text{Gain \%} = \left(\frac{y}{x} - 1\right) \times 100 = 25\%$$

Ans: Gain of 25%

15. The average of 25 numbers is 36.4. Find their sum. [1]

$$x_1 + x_2 + \dots + x_n = n\bar{x}$$

$$\text{Sum} = 25 \times 36.4 = 910$$

Ans: 910

16. A scooter covers 168 km in 4 hours. How much distance will it cover in 7 hours at the same speed? [2]

$$4 \text{ hours} \rightarrow 168 \text{ km}$$

$$7 \text{ hours} \rightarrow \frac{7}{4} \times 168 = 294 \text{ km}$$

Ans: 294 km

17. The speed of Sneha is 35 km/h and the speed of Priya is 56 km/h. Find the ratio of the times taken by them to cover the same distance. [2]

$$s_1 = \frac{d}{T_1}, s_2 = \frac{d}{T_2} \Rightarrow \frac{s_1}{s_2} = \frac{T_2}{T_1}$$

$$T_1 : T_2 = s_2 : s_1 = 56 : 35 = 8 : 5$$

Ans: 8 : 5

18. A train running at 90 km/h crosses a signal post in 12 seconds. Find the length of the train. [3]

$$\text{Speed} = 90 \times \frac{5}{18} = 25 \text{ m/s}$$

To cross a post, the train travels its own length.

$$\text{Length} = S \times T = 25 \times 12 = 300 \text{ m}$$

Ans: 300 m

19. Find the interest on ₹6000 for 2 years at 10% per annum (i) as simple interest, (ii) as compound interest, working year by year. [5]

$$\text{Interest for 1st year} = 6000 \times \frac{10}{100} = 600$$

(i) Simple interest: the 2nd year's interest is also 600, so S.I = $600 + 600 = 1200$

(ii) Compound interest: new principal = $6000 + 600 = 6600$

$$\text{Interest for 2nd year} = 6600 \times \frac{10}{100} = 660$$

$$\text{C.I} = 600 + 660 = 1260$$

Ans: (i) ₹1200 (ii) ₹1260

20. A sum of ₹6400 amounts to ₹7225 in 2 years at compound interest, compounded annually. Find the rate of interest per annum. [5]

$$A = P \left(1 + \frac{R}{100}\right)^n$$

$$7225 = 6400 \left(1 + \frac{R}{100}\right)^2$$

$$\Rightarrow \left(1 + \frac{R}{100}\right)^2 = \frac{7225}{6400} = \frac{289}{256} = \left(\frac{17}{16}\right)^2$$

$$\Rightarrow 1 + \frac{R}{100} = \frac{17}{16} \Rightarrow \frac{R}{100} = \frac{1}{16}$$

$$\Rightarrow R = 6.25\%$$

Ans: 6.25% per annum
